

Comments on and Errata for BIOS 662 Slides
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- Populations and Samples, Slide 37. Chebyshev's inequality should be

$$\Pr[\mu - K\sigma < Y < \mu + K\sigma] \geq 1 - \frac{1}{K^2}$$

E.g., if $K = 2$, then

$$\Pr[\mu - 2\sigma < Y < \mu + 2\sigma] \geq 0.75$$

- Point and Interval Estimation, Slide 42. Change $(y_{(7)}, y_{(17)})$ to $(x_{(7)}, x_{(17)})$.
- Point and Interval Estimation, Slide 45. Change $Z_{(r)}$ to $X_{(r)}$ twice.
- Point and Interval Estimation, Slide 46. Change $Z_{(r)}$ to $X_{(r)}$.
- Point and Interval Estimation, Slide 48. Change $(y_{(40)}, y_{(61)})$ to $(x_{(40)}, x_{(61)})$.
- Two Sample Tests, Part II, Slide 36. In class, we noted that the p-value for the two-sided permutation test was

$$p = \Pr[D \leq -15.75] + \Pr[D \geq 15.75] = 0.057 + 0.029 = 0.086.$$

This seems to contradict the result on the Slide 36 that we fail to reject at the $\alpha = 0.1$ level of significance. The discrepancy arises from using a symmetric critical region. Recall the critical region $C_{.1} = \{D : D = -15.75 \text{ or } D = 20.42\}$ was constructed so that the probability of being in each tail of the critical region was no more than 0.05, i.e., $\Pr[D \leq -15.75 | H_0] \leq 0.05$ and $\Pr[D \geq 20.42 | H_0] \leq 0.05$. More generally, we can write a symmetric critical region as $C_\alpha = \{D : D \leq d_{\alpha/2}^L \text{ or } D \geq d_{\alpha/2}^U\}$ where $d_{\alpha/2}^L$ is the largest real number such that $\Pr[D \leq d_{\alpha/2}^L | H_0] \leq 0.05$ and $d_{\alpha/2}^U$ is the smallest real number such that $\Pr[D \geq d_{\alpha/2}^U | H_0] \leq 0.05$. Alternatively, we could define a critical region $C_\alpha = \{D : |D| \geq d_\alpha\}$ by the smallest d_α such that

$$\Pr[|D| \geq d_\alpha | H_0] \leq \alpha.$$

This approach is valid since the type I error of the test does not exceed α . Note the critical region is not necessarily symmetric in the sense that probability of being in one of the tails of the critical region may exceed $\alpha/2$. Moreover, because we do not insist on symmetry, this approach can

be more powerful than employing a symmetric critical region. Using this approach applied to the problem in the notes, we get

$$C_{.1} = \{D : |D| \geq 15.75\} = \{D : D \in \{-17.5, -15.75, 20.42\}\},$$

such that we would reject at the $\alpha = .1$ level of significance, i.e., we now get a result consistent with the p-value of 0.086.

- Counting Data, Slide 57. Change p_1 to ρ_1 three times. Change p_2 to ρ_2 three times.
- Counting Data, Slide 58, first bullet. Change “is” to “in”.
- Poisson, Slide 10. First bullet. Change “of” to “we”.
- Regression II, Slide 12. Change $i = 2, \dots, n_2$ to $i = 1, \dots, n_2$.
- Regression II, Slide 44. Change “ k measures” to “ k independent measures”.
- ANOVA II, Slide 17. Note the multiplicity adjusted CIs are assuming a balanced design, i.e., $n_i = n$ for all i .
- ANOVA II, Slide 24. Change $N - k$ to $N - K$.
- ANOVA III, Slide 9. Change “less than” to “less than or equal to”.
- ANOVA III, Slide 14. The Box-Cox transformation can also be conducted using Proc Transreg in SAS.
- ANOVA III, Slide 25. Change $R_1 = 63$ to $R_1 = 63$, $R_2 = 32$ to $R_2 = 32$, and $R_3 = 25$ to $R_3 = 25$.
- Power and Sample Size III, Slide 3. Change alternative to $H_A : \mu_1 - \mu_2 = \delta_A > 0$.
- Rates and Proportions, Slide 28. Change V to \hat{V} four times.