Hint/Correction for Problem Set 1

3.5.1 We first need to make one more assumption (which was not included in the printed version but should have been) that

$$\int \dot{\ell}_{\tilde{\theta}} \dot{\ell}_{\tilde{\theta}}' p_{\tilde{\theta}} d\mu \quad \to \quad \int \dot{\ell}_{\theta} \dot{\ell}_{\theta}' p_{\theta} d\mu, \quad \text{as } \|\tilde{\theta} - \theta\| \to 0.$$
(1)

Now use (1) to show that

$$H(\tilde{\theta},\theta) \equiv \int \left(p_{\tilde{\theta}}^{1/2} - p_{\theta}^{1/2}\right)^2 d\mu \to 0, \text{ as } \|\tilde{\theta} - \theta\| \to 0.$$
 (2)

Next, show that (2) implies

$$\int |p_{\tilde{\theta}} - p_{\theta}| d\mu \to 0, \text{ as } \|\tilde{\theta} - \theta\| \to 0.$$
(3)

Finally, fill in the remaining steps to complete the problem (this is somewhat involved).